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## GATUNDU SUB COUNTY FORM FOUR 2018 EVALUATION EXAM

121/1
MATHEMATICS
PAPER I
JULY/AUGUST 2018
TIME: $2 ½$ HOURS

## INSTRUCTIONS TO CANDIDATES

(a) Write your name and index number in the spaces provided above
(b) Sign and write the date of exam in the space provided above.
(c) This paper consists of two section : section I and section II
(d) Answer all questions in section I and Only Five questions form section II
(e) All answers and working must be written on the question paper in the space provided below each question.
(f) Show all the steps in your calculation.
(g) Marks may be given for correct working even if the answer is wrong.
(h) Non -programmable silent electronic calculators and KNEC maths tables may be used except where stated otherwise.

Section 1

| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | Total |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |

Section II

| 17 | 18 | 19 | 20 | 21 | 22 | 23 | 24 | Total |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
|  |  |  |  |  |  |  |  |  |



GrandTotal

## Section 1 answer all questions in this section ( 50 marks)

1. Without using a calculator evaluate, $(3 \mathrm{mks})$
$1 / 2$ of $31 / 2+11 / 2(21 / 2-2 / 3)$
$3 / 4$ of $21 / 2+1 / 2$
2. Solve for x , given (3 Marks)
$\underline{27^{x-1}}=81^{2 x}$
$3^{2 x-1}$
3. The exterior angle of a regular polygon is equal to one - third its interior angle. Calculate the number of sides of the polygon and give its name. (3marks)
4. A bank in Kenya buys and sells foreign currencies as follows.
buying (Ksh)
1 Us dollar
1 sterling pound
1 sterling pound $\quad 142.41$

Selling (kshs.)
86.06
142.73

A tourist from united States of America converted 43521 US dollars into Kenya shillings.
i) Calculate the amount in Kenya shillings that she received
(ii)While in Kenya, the tourist spent sh. 2437821 and converted the balancetosterling pounds. How much in Sterling pound did the tourist receive to the nearest sterling pound?(3mks)
5. A Line passes through $A(1,1)$ and $B(x, y)$. The mid-point of $A B$ is $(3,5)$. If line $B C$ is perpendicular to $A B$, find the equation of line $B C$ in the form of $a x+b y+c=0$ (4mks)
6. A car park area in ashopping mall measuring 54 m by 72 m is covered by equal square tiles find the area in $\mathrm{m}^{2}$ of the largest size of the tiles if whole tiles are used. (3 marks)
7. A minor arc of a circle subtends an angle of $120^{\circ}$ at the centre of the circle. If the radius is 6.25 cm , find the length of the major arc giving your answer to 4 significant figures. (take $\pi=3.142$ ). ( 2 marks)
8. Two similar container hold $2000 \mathrm{~cm}^{3}$ and 6.75 litres respectively. If the smaller container is 15.5 cm in diameter, what is the radius of the larger container to 1 decimal place? ( 3 mks )
9. Simplify fully the expression
$\frac{6 x^{2}-9 x y-6 y^{2}}{8 x^{2}-2 y^{2}}$
10)Find the reciprocal of 20.95 to 4 decimal places using the tables of reciprocals. (1mark)

Hence evaluate $\frac{5}{20.95}$ without using mathematical tables or calculator.(2marks)
11)Write down the inequalities that define the unshaded region marked $R$ in the figure below. (3mks)

12) Use Logarithm tables to evaluate (4mks)
$\sqrt{\frac{32.4 \times 0.04352}{(5.24)^{2}}}$
13)Calculate the area of the shaded region below, given that $A C$ is an arc of a circlecentre $\mathrm{B} . \mathrm{AB}=\mathrm{BC}=14 \mathrm{~cm} \mathrm{CD}=8 \mathrm{~cm}$ and angle $\mathrm{ABD}=75^{0}$

14) A boy whose eye level when standing is 1.6 m , stands in front of a building 30 m tall. He observes the top of the building at an angle of elevation of $42^{\circ}$. Find the distance between the boy and the building leaving your answer correct to 4 significant figures. (3marks)
15)The figure below shows a sketch of a solid cuboid EFGHIJKL. Complete the sketch. (3mks)

16) Vector $\mathbf{p}$ passes through points $(10,20)$ and $(6,10)$ while $\mathbf{q}$ passes through points $(\mathrm{x}, 12)$ and $(-10,-18)$. If $\mathbf{p}$ and $\mathbf{q}$ are parallel, find x . (3 marks)

## SECTION (50 MARKS)

## Answer any five questions in this section in the spaces provided.

17.Atieno is a sales executive earning a salary of Ksh. 20,000 and a commission of $8 \%$ for the sales in excess of Ksh 100,000. If in January 2010 she earned a total of Ksh.48, 000 in salaries and commissions.
a) Determine the amount of sales she made in that month
(4 mks)
b) If the total sales in the month of February and March increased by $18 \%$ and then dropped by $25 \%$ respectively. Calculate
(i) Atieno's commission in the month of February
(ii) Her total earning in the month of March
18. (a) Find the inverse of the matrix (2 mks)
$\left[\begin{array}{ll}2 & 5 \\ 4 & 3\end{array}\right]$
(b) A transport company has two types of vehicles for hire: Lorries and buses. The vehicles are hired per day. The cost of hiring two lorries and five buses is Sh. 156,000 and that of hiring 4 lorries and three buses is Sh. 137,000.
(i) Form two equations to represent the above information. (2 mks)
(ii) Use matrix method to determine the cost of hiring a lorry and that of hiring a bus. (3 mks)
(c) Find the value of $x$ given that $\left[\begin{array}{cc}2 x-1 & 1 \\ x^{2} & 1\end{array}\right]$ is a singular matrix (3 mks)
19. a) The points $A(2,6), B(1,1) C(3,4)$ and $D(5,3)$ are vertices of a quadrilateral $A B C D$. Plot $A B C D$ on the grid below to form quadrilateral $A B C D$. (2 mark)

b) ABCD undergoes a rotation of positive $90^{\circ}$, about the origin. on the same grid, draw the image $A^{\prime} \mathrm{B}^{\prime} \mathrm{C}^{\prime} \mathrm{D}^{\prime}$ and state the coordinates of $\mathrm{A}^{\prime} \mathrm{B}^{\prime} \mathrm{C}^{\prime} \mathrm{D}^{\prime}$. (3 marks)
c) $A^{\prime} B^{\prime} C^{\prime} D^{\prime}$ undergoes a reflection in the $X$ - axis to give $A^{\prime \prime} B^{\prime \prime} C^{\prime \prime} D^{\prime \prime}$. On same grid, draw $\mathrm{A}^{\prime \prime} \mathrm{B}^{\prime \prime} \mathrm{C}^{\prime \prime} \mathrm{D}^{\prime \prime}$ and state the coordinates of $\mathrm{A}^{\prime \prime} \mathrm{B}^{\prime \prime} \mathrm{C}^{\prime \prime} \mathrm{D}^{\prime \prime}$

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(3 marks)
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d) $A$ " $B^{\prime \prime} C " D "$ is the image of $A B C D$ under a reflection. On the grid, mark the mirror line and state its equation.
20. The figure below shows a bucket of depth 30 cm used to fill a cylindrical tank of radius 1.2 m and height 1.35 m which is initially three-fifth full of water.

## Calculate;


(a) The capacity of the bucket in litres
21.) Forty students in a form 2 class were weighed and their masses recorded to the nearest kilogram as shown below.

|  | 45 |  | 48 |  | 56 |  | 39 |  | 47 |  | 36 |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 45 |  | 37 | 46 |  | 35 |  | 43 |  | 51 |  | 42 |
|  | 47 |  | 47 |  | 40 |  | 46 |  | 41 |  |  |  |
| 45 |  | 43 |  | 46 |  | 54 |  | 42 |  | 51 |  | 39 |
|  | 42 |  | 45 |  | 44 |  | 49 |  | 50 |  | 46 |  |
| 39 |  | 42 |  | 48 |  | 50 |  | 38 |  | 45 |  | 35 |

a) Starting with the class 35-39 tabulate this data in a frequency table
(2marks)
b) Find the modal frequency
c) calculate the mean mass of the students
d)Estimate the median mass
22.)Four ships are at sea such that a streamliner $S$ is 150 km on a bearing of $025^{\circ}$ from a cargo
ship C. A trailer T is 300 km on a bearing of $145^{\circ}$ from the cargo ship and a yacht Y is due West of C and on a bearing of $300^{\circ}$ from T .
a) Using a scale of $1 \mathrm{~cm}=50 \mathrm{~km}$, draw on accurate scale drawing showing the positions of S, C, T and Y
(4marks)
b) By measurement from your scale drawing determine:
i) The distance and bearing of Y from $S$ (2marks)
ii) The distance ST (2marks)
iii) The distance YT (2marks)
23)In a triangle $\mathrm{OAB}, \mathrm{M}$ and N are points on OA and OB respectively, such that $\mathrm{OM}: \mathrm{MA}=2: 3$ and $O N: N B=2: 1$. $A N$ and $B M$ intersect at $X$. Given that $O A=\mathbf{a}$ and $O B=\mathbf{b}$
(a) Express in terms of $\mathbf{a}$ and $\mathbf{b}$ :-
(i) $\mathbf{B M}$ (1mark)
(ii) AN(1mark)
(b) Taking $\mathrm{BX}=\mathrm{kBM}$ and $\mathrm{AX}=\mathrm{hAN}$ where $\mathbf{k}$ and $\mathbf{h}$ are constants express $\mathbf{O X}$ in terms of (i) $\mathbf{a}, \mathbf{b}$ and $\underset{\sim}{\mathbf{k}}$ only (2marks)
(ii) $\mathbf{a}, \mathbf{b}$, and $\mathbf{h}$ only (2marks)
(c) Use the expressions in (b) above to find values of $\mathbf{k}$ and $\mathbf{h}$ (4marks)
24) The table below gives some values of $X$ and $Y$ for the function $y=\frac{1}{2} x^{2}+2 x+1$ in the interval $0 \leq x \leq 6$
a) Complete the values in the table below(2marks)

| X | 0 | 1 | 2 | 3 | 4 | 5 | 6 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Y |  |  | 7 |  |  | 23.5 |  |

b) Using the values, estimate the area bounded by the curve, x -axis , y -axis and the line $\mathrm{x}=6$ by the trapezium rule , use 6 trapezia (3marks)
c) By integration, calculate the exact area bounded in (a) above (3marks)
d) Find the percentage error made, when the trapezium rule is used, to 2.d.p (2mks)

