NAIROBI SCHOOL

Opener Exam, Term 2

121

MATHEMATICS

Form 4



Question Paper

July. 2022—150 minutes

FILL IN YOUR PERSONAL DETAILS HERE									
Student Name:									
Admission Number:		Class:	4						

Instructions to candidates

- (a) Write your name, admission number and class in the spaces provided above.
- (b) This paper consists of two sections; Section I and Section II.
- (c) Answer all the questions in Section I and any five questions from Section II.
- (d) Show all the steps in your calculations, giving your answers at each stage in the spaces provided below each question.
- (e) KNEC Mathematical tables may be used, except where stated otherwise.
- (f) Non-programmable silent electronic calculators must not be used, except where stated otherwise.
- (g) This paper consists of 16 printed pages.
- (h) Remember to tick the questions you have attempted in Section II

For Examiner's Use Only

SECTION I

1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	TOTAL

SECTION II(Please tick the questions you have attempted)

17	18	19	20	21	22	23	24	TOTAL
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TURN OVER

SECTION ONE - 50 MARKS

Answer all questions from this section in the spaces provided.

1). Solve
$$2\sin^2\theta + 3\cos\theta = -1$$
 for $0^\circ \le \theta \le 360^\circ$

(3 marks)

2). Given that
$$A = \sqrt[4]{\frac{d-c^2g}{b+c^2f}}$$
 make **c** the subject of the formula. (3 marks)

3). A sum of Ksh. 8000 was partly lent at 10% p.a simple interest and 12.5% p.a simple interest. The total interest after 2 years was Ksh. 1775. How much was lent at 10% simple interest? (3 marks)

4). Solve the following simultaneous equations

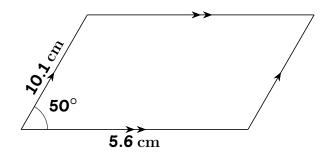
(4 marks)

$$\log_3(3x + 4y) = 2$$

$$\log_2(2x+y)=1$$

5). The position vectors for points \mathbf{P} and \mathbf{Q} are $6\mathbf{i} - 3\mathbf{j} + 9\mathbf{k}$ and $3\mathbf{i} - 6\mathbf{j} - 3\mathbf{k}$ respectively. \mathbf{R} divides line \mathbf{PQ} in the ratio $\mathbf{1}:\mathbf{2}$. Find the position vector of \mathbf{R} and express it in terms of unit vector \mathbf{i} , \mathbf{j} and \mathbf{k} . (3 marks)

6). The parallelogram below has adjacent sides of lengths 5.6 cm and 10.1 cm respectively while the angle between them is 50° .



Calculate the percentage error of finding its area.

(3 marks)

7). Simplify completely $\frac{9x^2 - 16x + 7}{162x^2 - 98}$

(3 marks)

8). Without using mathematical tables or a calculator, express $\sin 45^\circ$ in surd form. Hence simplify $\frac{\sqrt{8}}{1+\sin 45^\circ}$ leaving your answer in surd form. (3 marks)

9). (a) Expand $\left(1 - \frac{1}{4}x\right)^5$ up to the 4^{th} term.

(2 marks)

(b) Use the expansion in part (a) above to find the approximate value of $(1.25)^5$. (2 marks)

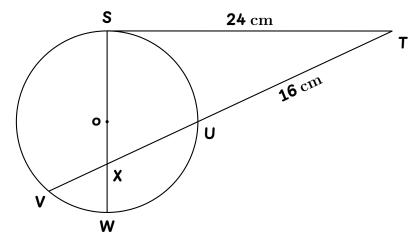
10). A bus travelling at an average speed of $x \, \mathrm{km/h}$ left a station at $8.15 \, \mathrm{a.m}$. A car, travelling at an average speed of $80 \, \mathrm{km/h}$ left the same station at $9.00 \, \mathrm{a.m.}$ and caught up with the bus at $10.45 \, \mathrm{a.m.}$ Find the value of $x \, \mathrm{cm/h}$ (3 marks)

11). The data below represents the ages in months at which 6 babies started walking;
9,11,12,13,11 and 10. Without using a calculator, find the exact value of the variance of the data.
(3 marks)

12). A triangle PQR has an area of $3.2~\rm cm^2$. It's image under a transformation matrix $\begin{pmatrix} 4x^2 & 5 \\ -x & 1 \end{pmatrix}$ has an area of $19.2~\rm cm^2$. Find the value of x (3 marks)

13). The scale of a map is given as 1:50,000. Find the actual area in hectares of the region represented by a rectangle of sides $6\,\mathrm{cm}$ by $7\,\mathrm{cm}$. (3 marks)

14). In the figure below, the tangent ST meets chord VU produced at T. chord SW passes through the centre O of the circle and intersects chord VU at X. line ST = 24 cm and UT = 16 cm.



(a) Calculate the length of chord ${\bf VU}$.

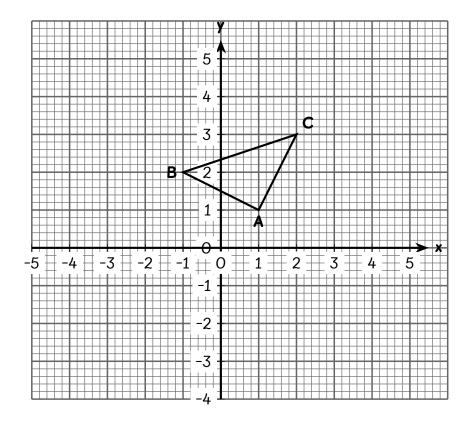
(1 mark)

(b) If $\mathbf{WX} = \mathbf{6} \ \mathrm{cm}$ and $\mathbf{VX} : \mathbf{XU} = \mathbf{2} : \mathbf{3} \ \mathrm{find} \ \mathbf{SX}$

15). Find the value of ${f x}$ in the following equation, ${f 2^{2x-1}}+{f 4^{x+1}}={f 36}$

(3 marks)

16). Triangle ABC is shown on the coordinate plane below. Given that A(1,1) is mapped onto A'(1,-1) by a shear with the y-axis invariant, draw triangle A'B'C' the image of triangle ABC under the shear. (3 marks)



SECTION TWO - 50 Marks

Answer any **five** questions from this section in the spaces provided.

17).	(a) The probability that Nina goes to bed on time is $3/4$. If she goes to bed on time probability that she wakes up on time is $2/3$, otherwise the probability that she way up on time is $1/4$. If she wakes up late, her probability of getting to class on time is $1/5$ otherwise her probability of getting to class on time is $1/5$. Find the probability of getting to class on time is $1/5$.	vakes ime is		
	that: (i) She wakes up late.	(3 marks)		
	(ii) She gets to class on time	(3 marks)		
	(b) A die and a coin are cast simultaneously. (i) Draw a table to show all the possible outcomes	(2 marks)		
	(ii) What is the probability of a tail and a number less than 4 showing up.	(2 marks)		

- 18). (a) The first term of an arithmetic progression (AP) is 6. The sum of the first 7 terms of the AP is 126.
 - (i) Find the common difference of the AP

(2 marks)

(ii) Find the 19th term of the AP.

(1 mark)

- (b) The 2^{nd} , 3^{rd} and 11^{th} terms of an increasing arithmetic progression(AP) form the first 3 terms of a geometric progression (GP). The first term of the AP is -2.
 - (i) Find the common difference of the AP and the common ratio(r) of the GP. (4 marks)

(ii) Find the sum of the first 5 terms of the geometric progression(GP).

(3 marks)

- 19). An aircraft leaves town $P(30^{\circ}\mathrm{S}, 17^{\circ}\mathrm{E})$ and flies due north to $Q(60^{\circ}\mathrm{N}, 17^{\circ}\mathrm{E})$. It then flies at an average speed of 300 knots for 8 hours due west to town R. Determine:
 - (a) The distance PQ in nautical miles.

(2 marks)

(b) The position of town \mathbf{R} .

(4 marks)

(c) The local time at $\bf R$ if the local time at $\bf Q$ is $\bf 3.12~pm$.

(2 marks)

(d) The distance travelled by the aircraft from \bm{Q} to \bm{R} to the nearest kilometre. (1 $km=\bm{0.539957}$ nm)

 $\frac{\sin 2x}{3\cos x - 2}$

120°

-0.87

-3.5

-0.5

20). (a) Complete the table below, giving the values correct to 2 decimal places.

-2

30°

0.60

1

60°

0.87

ecima	l place	(2 marks)			
240°	270 °	300°	330°	360°	
0.87				0	

1

(b) On the grid provided, draw the graphs of $y = \sin 2x$ and $y = 3\cos x - 2$ for $0^{\circ} \le x \le 360^{\circ}$ on the same axes. Use a scale of 1 cm to represent 30° on the x-axis and 2 cm to represent 1 unit on the y-axis. (5 marks)

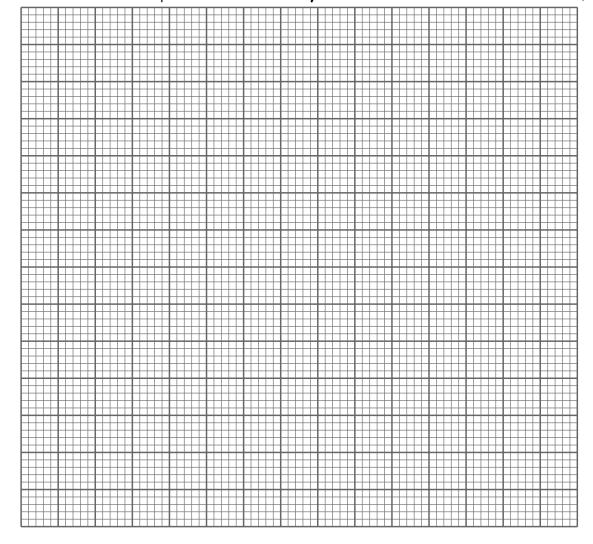
150°

180°

210°

0.87

-4.60



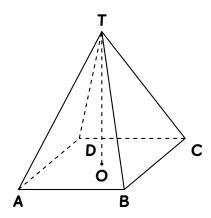
(c) Use the graph in **(b)** above to solve the equation $3\cos x - \sin 2x = 2$.

(2 marks)

(d) State the amplitude of $y = 3 \cos x - 2$.

(1 mark)

21). The figure below is of a right pyramid on a rectangle base. TC = TB = TA = TD = 17 cm, and TO = 15 cm. AB is twice BC.



Calculate:

(i) The length AB

(4 marks)

(ii) The angle between TC and plane ABCD

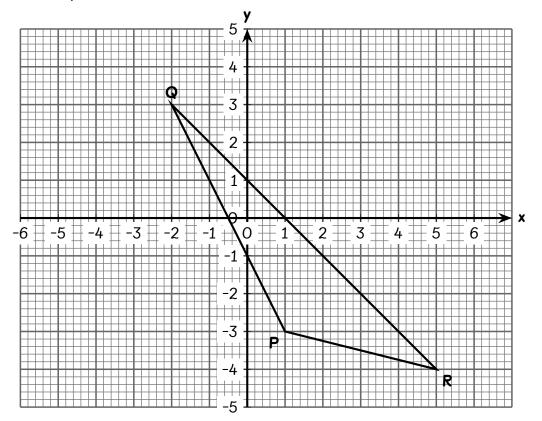
(2 marks)

(iii) The angle between **TD** and plane **TAC**

(2 marks)

(iv) The angle between TAB and ABCD

22). (a) Given that point $\mathbf{Q}(-2,3)$ is mapped onto $\mathbf{Q}'(4,3)$ by a shear with $\mathbf{x}-\mathbf{axis}$ invariant,



(i) Draw triangle P'Q'R', the image of PQR under the shear.

(3 marks)

 $\begin{picture}(ii)\end{picture}$ Determine the matrix representing the shear.

- (2 marks)
- (b) Triangle P'Q'R' is mapped onto triangle P''Q''R'' by a transformation defined by the matrix $\begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix}$

(i) Draw triangle P"Q"R"

(3 marks)

(ii) Find a combined matrix that maps PQR onto P''Q''R''

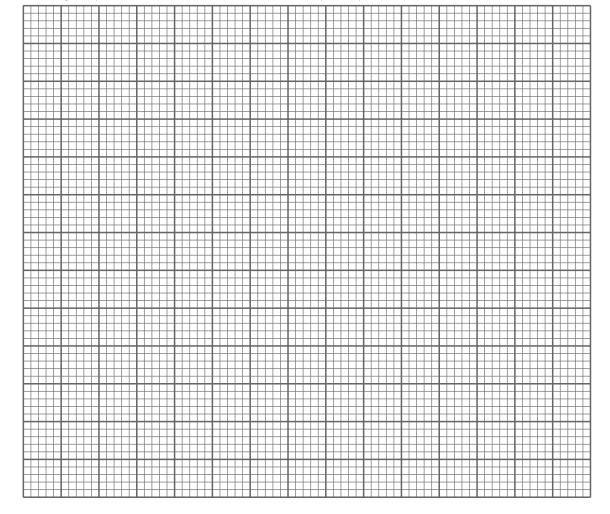
23). The table below shows the masses in kg of **50** animals selected at random in a farm.

60	25	37	50	62	39	47	64	70	58
66	48	28	47	43	56	59	53	77	46
47	59	40	78	45	51	61	73	33	70
69	61	52	53	36	48	74	58	82	54
54	68	41	59	45	69	83	50	91	63

(a) Starting with the mass of **25** and using equal class intervals of **10**, make a frequency distribution table for the data. **(2 marks)**

(b) On the grid provided draw a cumulative frequency curve for the data.

(4 marks)



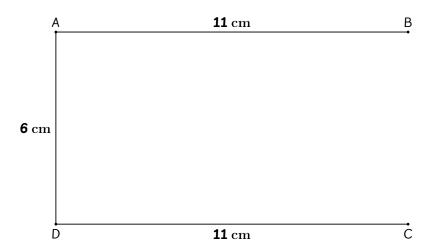
(c) Use the graph in **(b)** above to determine:

(i) The median mass.

(2 marks)

(ii) The quartile deviation.

24). The diagram below is a scale drawing of a piece of land. Three boundaries AB, AD and DC of the land are given. The fourth boundary is not given but it is known that the area of the land if greater than that of rectangle ABCD.



Use a ruler and pair of compasses only in this question.

(a) Construct the locus of all points equidistant from points ${\bf B}$ and ${\bf C}$.

(1 mark)

- (b) The locus of any point **P** lying on the fourth boundary is such that $\angle BPC = 45^{\circ}$. Draw the fourth boundary. (4 marks)
- (c) Shade the region within the scale drawing in which a variable point **X** must lie giving that **X** satisfies the following conditions. (5 marks)
 - (i) \boldsymbol{X} is at least $\boldsymbol{1}$ cm from each of the four boundaries
 - (ii) X is at least 6 cm from A
 - (iii) Area of $\triangle AXD \geq 15~\mathrm{cm}^2$