THE MOKASA II JOINT EXAMINATION.

Featuring Kenya Certificate of Secondary Education (K.C.S.E.) 2024.

121/2

MATHEMATICS

Paper 2

ALT A FORM FOUR MOCK

July/August. 2024- $2\frac{1}{2}$ hours

NAME.....

CLASS......DATE.....DATE......DATE......

Instructions to candidates

- (a) Write your name and admission number in the spaces provided above.
- (b) Sign and write the date of examination in the spaces provided.
- (c) This paper consists of two sections: Section I and Section II.
- (d) Answer all questions in section I and only five questions from section II.
- (e) Show all the steps in your calculations, giving the answers at each stage in the spaces provided below each question.
- (f) Marks may be given for correct working even if the answer is wrong.
- (g) Non-programmable silent electronic calculators and KNEC mathematical tables may be used, except where stated otherwise.
- (h) This paper consists of 16 printed pages.
- (i) Candidates should check the question paper to ascertain that all the pages are printed as indicated and that no questions are missing.
- (i) Candidates should answer the questions in English.

For Examiner's Use Only

Section I

1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	Total

Section II

17	18	19	20	21	22	23	24	Total

Grand Total

the talk	

SECTION I (50 marks)

Answer all the questions in this section in the spaces provided.

1. The expression ax^2 -60x + 18 is a perfect square, where ais a constant. Find the value of a.

2. A rectangular plot of land has length of 125.8 m and an exact width of 84 m. Find the percentage error in calculating area of the plot correct to 3 decimal place. (3 marks)

Min A = 125.75 x 84 = 10563 Actual L = 125.8 x 84 = 10567.2 L. F = 10571.4-10563

$$R \cdot E = 4.2$$

$$R \cdot E = 4.2$$

$$10567.2$$

$$M$$

$$M = (4.2 \times 100)$$

$$10567.2$$

$$-0.040$$

3. Find the area of a sector of radius 10.5cm subtended by an angle of $\frac{1}{3}\pi^c$ at the center.

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4. Without using a calculator or mathematical tables, evaluate;

$$\frac{1}{12} + \frac{1}{12} \times \frac{1}{12}$$

(3 marks)

$$456+12$$

$$= 56+3 \checkmark 4$$

$$= \frac{16+3}{2}$$

5. Simplify the logarithmic expression;

Log (25 X5)
$$V_{M}$$

$$\frac{125}{25} M$$

(3 marks)

6. A man who deposited Sh.50,000 in an investment account compounded semi-annually had at a total amount of Sh.70,925 after three years. Calculate the rate of interest per annum to the nearest whole number.

marks)

0.059997619= 700

7. A quantity P is partly constant and partly varies as the square of Q. If Q = 2 when P = 9 and Q = 4 when P = 33, find the value of P when Q = 1.5.

(4 marks) $P = K + MQ^{2}M$ K = 1 9 = K + 4M $P = 1 + 2Q^{2}$

$$M = 2$$

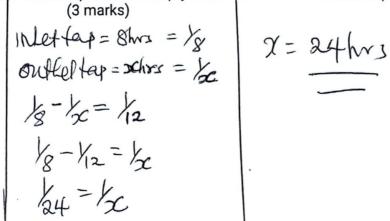
 $9 = K + 8$
 $K = 1$
 $P = 1 + 2Q^{2}$
 $P = 1 + 2(1-s)^{2}$
 $P = 5.5$

8. Expand $(3x-y)^4$ and simplify hence evaluate $(1.5-0.2)^4$. (4 marks) (3x-y) = (3x) (4), (3x) (4) (3x) (4)2, (3x) (4)3 (3x) (-4)4 M 3X = 1.5 $81(0.5)^{4} - 108(0.5)^{3}(0.2) + 54(0.5)^{2}(0.2)^{2} - 12(0.5)(0.2)^{3} + (0.2)^{2}$ X = 0.5 = 2.8561 \times \times

9. A committee of 3 people is to be chosen randomly from 5 men and 3 women. If every gender must be represented in the committee, find the probability of choosing more women than men.

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10. An inlet tap can fill an empty tank in 8 hours. It takes 12 hours to fill the tank when the inlet tap and an outlet tap are both opened at the same time. Calculate the time the outlet tap takes to empty the full tank when the inlet tap is closed.

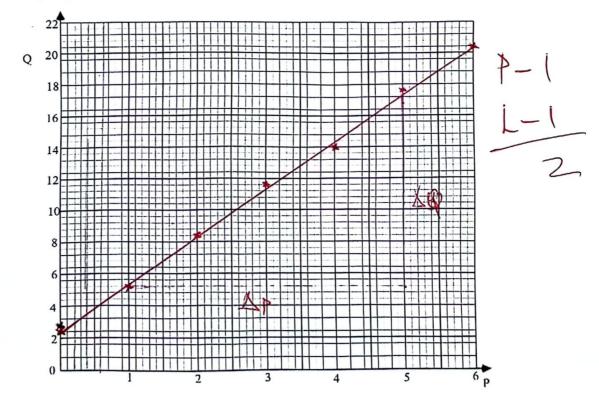


11. The table below shows the relationship between the quantities P and Q.

Р	0	1	2	3	4	5	6
Q	2.4	5.2	8.4	11.6	14.0	17.6	20.4

(a) On the grid provided, draw a line of best fit.

(2 marks)



(b) Using the graph, find the law connecting P and Q.

(1 mark)

12. Solve the equation $8\sin^2 x = 12\cos x$ for $Q \le x \le 360^0$.

85 In
$$X - 12(0SX = 0)$$

87 $^{2} + 129 - 8 = 0$

87 $^{2} + 39 - 2 = 0$

87 $^{2} + 39 - 2 = 0$

87 $^{2} + 49 - 9 - 2 = 0$

87 $^{2} + 49 - 9 - 2 = 0$

87 $^{2} + 49 - 9 - 2 = 0$

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87 $^{2} + 49 - 9 - 2 = 0$

88 $^{2} + 12(0SX = 0)$

89 $^{2} + 129 - 8 = 0$

29 $^{2} + 49 - 9 - 2 = 0$

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29 $^$

$$8^{4}y^{2} + 12y - 8 = 0$$

$$2y^{2} + 3y - 2 = 0$$

$$2y^{2} + 4y - y - 2 = 0$$

$$2y(y+2) - 1(y+2) = 0$$

$$(2y-1)(y+2) = 0$$

whose area is 36 cm². Given that the matrix of the transformation is $\binom{4}{2}$ the value of x. (3 marks)

$$\frac{36}{6} = 4x - 2(x-1) \text{ My}$$
 $6 = 4x - 2x + 2 \text{ My}$
 $2x = 4$
 $2x = 4$

14. The gradient of curve at any given point is given by $2x^2 - 4$, given that the curve passes through (1, 2), find the equation of the curve. (3 marks)

$$\frac{dy}{dx} = 2x^{2} - 4$$

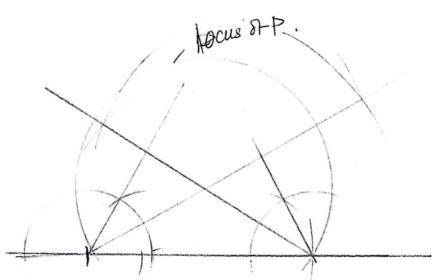
$$y = \sqrt{2x^{2} - 4} dx \sqrt{m}$$

$$y = \sqrt{2x^{2} - 4x} + C \left(\frac{1}{2}\right)^{n}$$

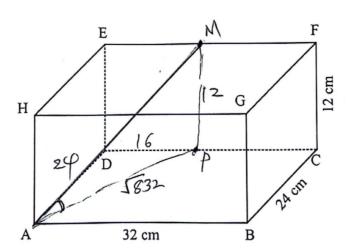
$$2 = 2x^{2} - 4 + C$$

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15. AB is a fixed line segment 6cm long. Point P moves on one side of the plane of AB such that ${\sf APB}$ is always ${\sf 60}^{\sf 0}$. Construct the locus of P. (3 marks)



16. The figure below represents a cuboid ABCDEFGH. AB = 32 cm, BC = 24 cm and CF = 12 cm.



Given that M is the mid-point of EF, calculate the angle between AM and plane

ABCD, correct to 2 decimal places.

(3 marks)

$$AP = \sqrt{24^2 + 16^2} \text{ my } \theta = 4an^{-1} \left(\frac{1^2}{1832}\right)$$
 $= \sqrt{832} \text{ my } \theta = 22.59^{\circ} \text{ M}$
 $AP = \sqrt{832} \text{ my } \theta = 4an^{-1} \left(\frac{1^2}{1832}\right)$
 $= \sqrt{832} \text{ my } \theta = 22.59^{\circ} \text{ M}$

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SECTION II (50 marks)

Answer only five questions from this section in the spaces provided.

17. The table below shows income tax rates for the year 2023

Taxable Income in K shs per month	Tax Rate (%) per month
1 15000	0
15001 27000	10
27001 37000	15
37001 45000	20
45001 50000	25
Above 50000	30

In November 2023, Silas earned a basic salary of Sh. 38 320. In addition, he was entitled to a house allowance of Sh. 12 800 per month and medical allowance of Sh. 6 850. He also has a non - taxable risk allowance of Sh. 5 000 per month. He contributes to a provident fund of Sh. 3 500. He also has tax relief of Sh. 1 480 monthly.

(2 marks) (a) Calculate Silas' taxable income in that month. Taxable Income = 38 320+12800+6850 Mg = Sh. 57 970 VA

(b) Calculate Silas' Pay As You Earp (P.A.Y.E) for November 2023. (5 marks)

79 70 × 3% = 2391,4

Gross 60x = 1250 +1500 +1600 + 1250 +2391

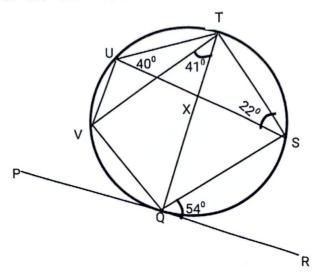
 $|2000 \times |0| = |200|$ $|10,000 \times |5| = |500|$ $|10,000 \times |5|$ $|10,000 \times |5| = |500|$ $|10,000 \times |5| = |500|$ $|10,000 \times |5|$

(c) In the month of December 2023, Silas' tax in the last band was Sh. 2 556. Calculate his net salary in December.

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18. In the figure below PQR is a tangent to the circle at point Q <SQR = 54° , <VTQ = 41° <UST = 22° and <SUT = 40° .



Giving reasons, find the value of

(i) <PQV, 41°, fingle subtended by a Chord QV to the accounterence is the same as the angle formed by the chord QV and tangent PQR.

(ii) <UVT
22°, Engles subtended by the Same chord UT to
the circumference on the Same segment.

- (iii) <PQT L-TQS = 40' angles stublended by same chora.

 Inflec in a straight
- (iv) «suv = 95° opposite angle in a cyclic guadalateral Vasu add up to 180°.
- (v) <0xs 76° sum angles in the triangle QXS add up to 180°.

- 19.(a) The first term of an Arithmetic Progression (AP) is 3. The sum of the first 6 terms AP is 78. of the
 - Find the common difference of the AP. $78 = 6/2(2x^3+(6-1)d)$ M 78 = 18 + 15d 15d = 60 A d = 4

(ii) Given that the sum of the first n terms of the AP is 406, find n.

(2 marks)

Given that the sum of the sum of

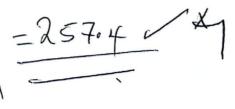
- (b) The 2nd, 4th and 7th terms of another AP form the first th Progression (GP). If the common difference of the AP is 2, find;
 - (i) , The first term of the GP;

The first term of the GP; a+d, a+3d, a+6d a+3d = a+6d = a+6d = a+3d a+3d = a+3d = a+3d a+3d a+3d a+3d a+3d a+3d a+3d a

The sum of the first 7 terms of the GP, to 4 significant figures.

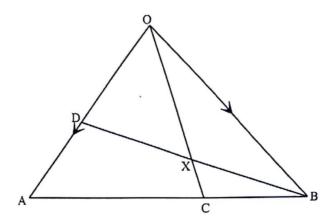
$$S_{7} = \frac{\alpha(8^{n}-1)}{7^{-1}} = \frac{3}{8}$$

$$= \frac{3(1.5^{7}-1)}{1.5^{-1}}$$



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20. In the figure below C is a point on AB such that BA = 3BC and D is the mid - point of OA. OC and BD intersect at X. Given that OA = a and OB = b.



(a) Write down in terms of a and b the vectors;

(1 mark)

(2 marks)

(iii) BD

$$BD = BA + AB$$

 $= 9 - 5 - 29$ $= 29 - 5$

(1 mark)

(b) If BX $\Longrightarrow h$ BD, express $\emptyset X$ in terms of **a**, **b** and h.

(c) If 0x = k0c, find h and k. $0X = K(\frac{1}{3}2 + \frac{1}{3}k)$ $0X = \frac{1}{3}K2 + \frac{1}{3}K2$ $1 = \frac{$

how that B, X and D are collinear.

BD = 12 - 5 | BX = 12 BD BX | BD with point B common BX = 12 (2 mark)

BX = 12 (2 mark)

BX = 12 BD BX | BD with point B common BX = 12 (2 mark)

BX = 12 (2 mark)

BX = 12 BD BX | BD with point B common BX = 12 (2 mark)

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21. Triangle A'B'C' is the image of triangle ABC with vertices A(3,-1), B(1,3) and C(4,2) transformation represented by matrix $M = \begin{pmatrix} -0.6 & -0.8 \\ -0.8 & 0.6 \end{pmatrix}$

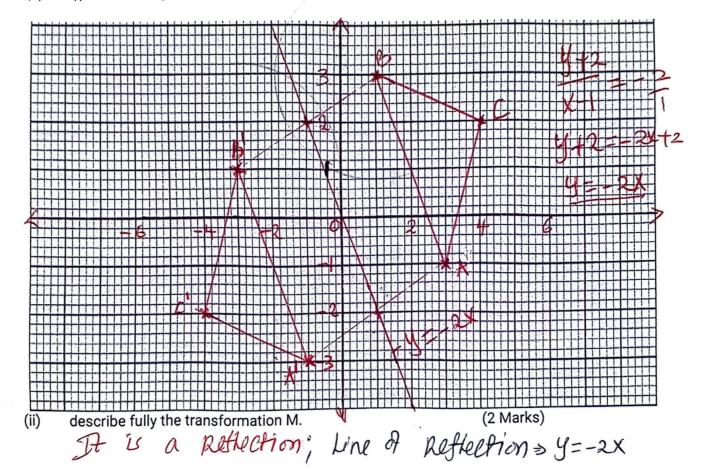
(a) Find the coordinates of triangle A'B'C'.
$$\begin{pmatrix}
-6 & 6 & -0.8 \\
-0.8 & 0.6
\end{pmatrix}
\begin{pmatrix}
A & B & C \\
3 & 1 & 4 \\
-1 & 3 & 2
\end{pmatrix} = \begin{pmatrix}
A & B & C \\
-1 & -3 & -4 \\
-3 & 1 & -2
\end{pmatrix}$$

$$\begin{pmatrix}
A & B & C \\
-1 & -3 & -4 \\
-3 & 1 & -2
\end{pmatrix}$$

$$\begin{pmatrix}
A & B & C \\
-1 & -3 & -4 \\
-3 & 1 & -2
\end{pmatrix}$$

$$\begin{pmatrix}
A & B & C \\
-1 & -3 & -4 \\
-3 & 1 & -2
\end{pmatrix}$$

on the grid below draw Triangles ABC and A'B'C'. (b)



Triangle A"B"C" is the image of triangle A'B'C' and a transformation represented (c) by the matrix $N = \begin{pmatrix} 2 & -1 \\ -4 & 3 \end{pmatrix}$

(i) Find the coordinates of Triangle A"B"C" $\begin{pmatrix}
2 & -1 \\
-4 & 3
\end{pmatrix}
\begin{pmatrix}
+1 & |3| & |2| \\
-1 & -3 & -4 \\
-3 & 1 & -2
\end{pmatrix} = \begin{pmatrix}
+1 & |B| & |2| \\
1 & -7 & -6 \\
-5 & 15 & 10
\end{pmatrix}$ $+1 \begin{pmatrix}
1 & -5 & |3| & |4| & |4| \\
1 & -5 & |3| & |4| & |4| \\
-5 & |3| & |4| & |4| & |4| & |4|
\end{pmatrix}$ $+1 \begin{pmatrix}
7 & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| & |4| &$

Determine a single matrix that maps triangle ABC onto triangle A"B"C".

- 22. The position of two towns P and Q are given as P(40°N,10°W) and Q(40°N,170°E). (use $\pi = \frac{22}{7}$, Radius of the Earth = 6371km).
- (a) Find the difference in longitude between the two towns. (1 mark)

(b) Find the shortest distance from P to Q in Kilometres correct to two decimal places. (2 ma (2 marks)



(c) (i) A ship sailed from town P towards town R which is directly east of P covering a distance of 2000km. Determine the position of R.

(ii) If the ship departed P at 2.00pm, sailing at an average speed of 150 knots,

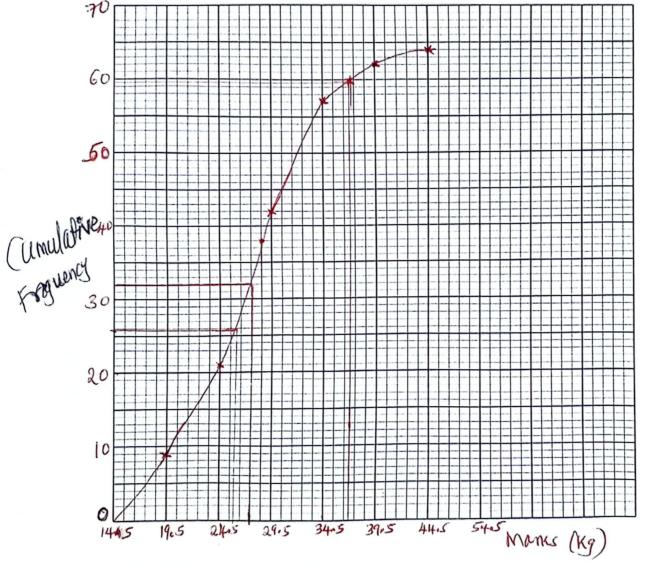
 $T = D = \begin{cases} T = (1079.33) \\ 150 \end{cases}$ $T = (1079.33) \begin{cases} T = (1079.33) \\ 150 \end{cases}$ $T = (1079.33) \begin{cases} T = (1079.33) \\ 150 \end{cases}$ $T = (1079.33) \begin{cases} T = (1079.33) \\ 1079.33 \end{cases}$ $T = (1079.33) \begin{cases} T = (1079.33) \\ T = (1079.33) \end{cases}$ $T = (1079.33) \end{cases}$

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23. The masses of 64 hybrid goats in a ranch in Laikipia were recorded as follows:

Mass in kg	15 19	20 24	25 29	30 34	35 39	40 44
No. of goats	9	12	21	15	5	2
CF	9	21	42	57	62	64

(a) On the grid provided, draw a cumulative frequency curve to represent the above information. (4 marks)



P- 2

C-1

S-1

(b) Use your graph to estimate:

i) The median

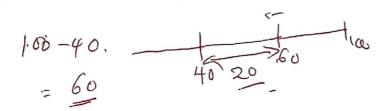
(1 mark)

The number of goats that were overweight if 36 kg is the recommended ii) (2 marks) healthy weight.

64-60

The range of weight of the middle 40% of the goats. iii) marks)

(3



0-40.

60 Apercuntile & 40 Apercentile.

X64)

404 = (400000)

-> 28.5 26-28.5

- 24. The dimensions of a rectangular flow of a proposed room are such that
 - The length is greater than the width but at most twice the width
- The sum of the width and length is more than 4 meters but less than 10 meters

If x represents the width and y the length.

Write inequalities to represent the above information.

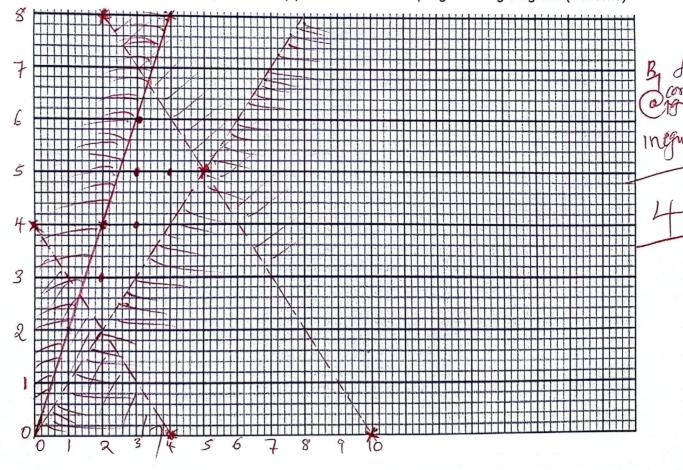
(4 marks)

962X X+Y74

X44710

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(b)Represent the inequalities in (a) above on a linear programming diagram. (4 marks)



Using the integral values of x and y, list all the possible dimensions of the (2 marks) Junes floor hence find the maximum possible area of the floor.

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